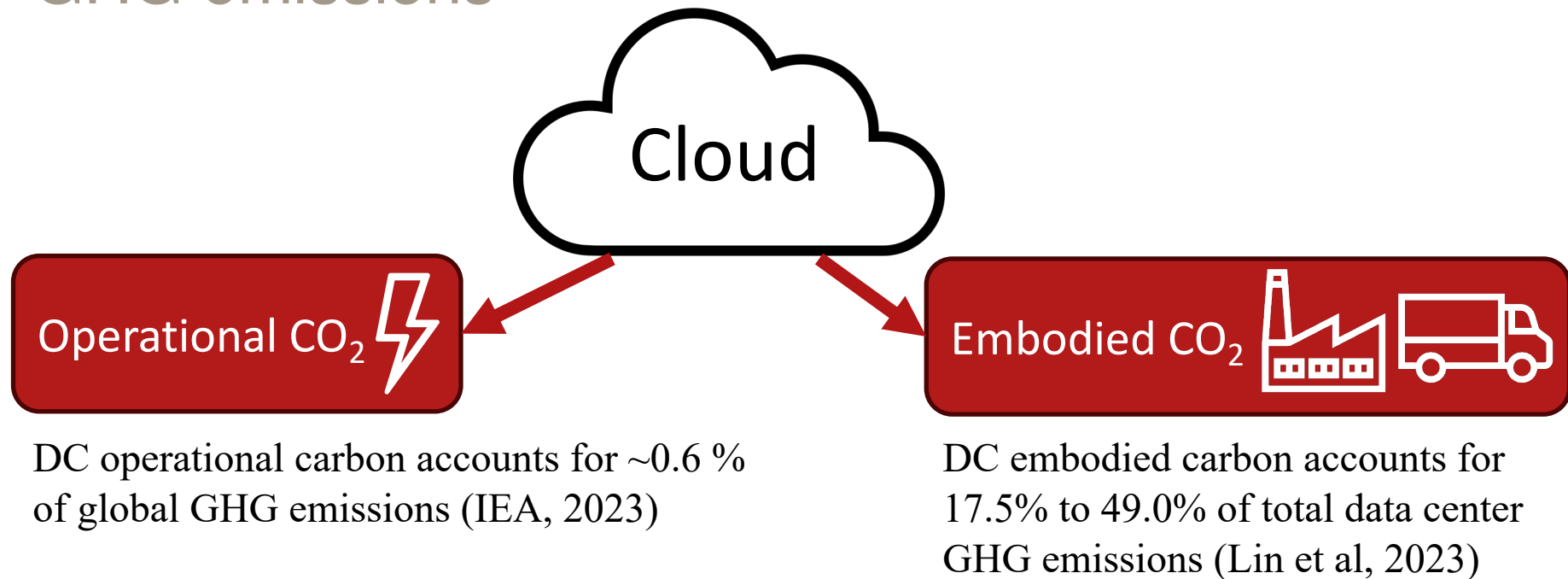


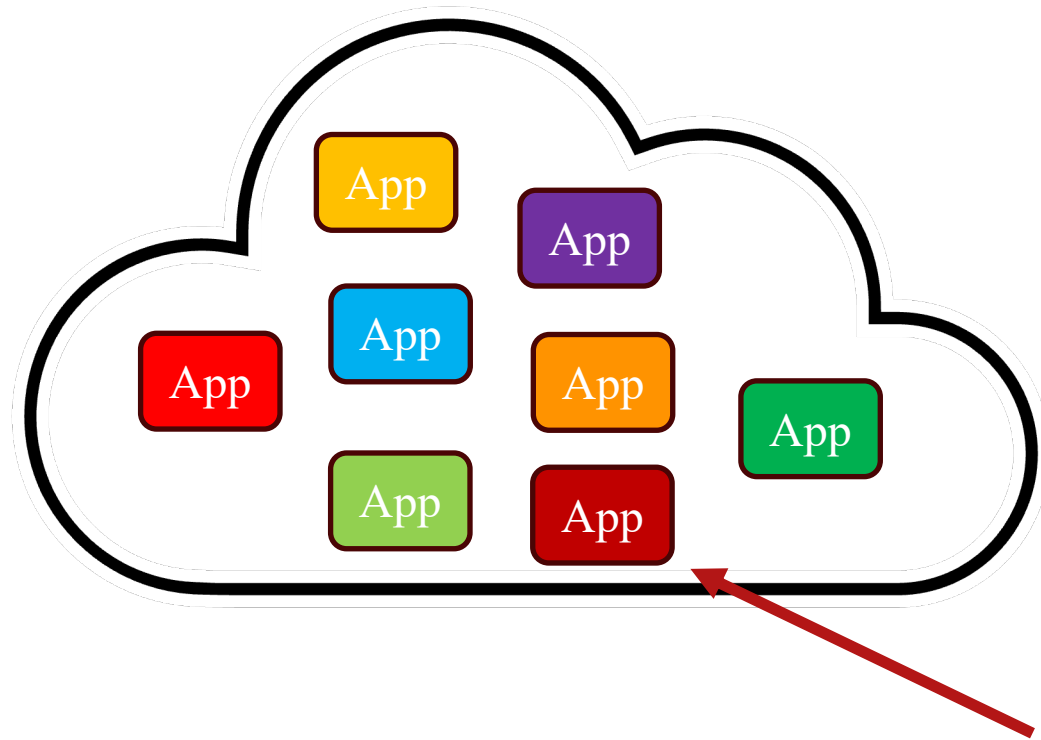
Towards Game-Theoretic Approaches to Attributing Carbon in Cloud Data Centers

Leo Han, Jash Kakadia, Benjamin C. Lee, Udit Gupta

Data centers (DCs) account for $>0.6\%$ of global GHG emissions



Data center capacity is projected to grow 10% year-on-year (McKinsey, 2023)



What is the carbon footprint of **App** ?

Cloud carbon attribution is increasingly important

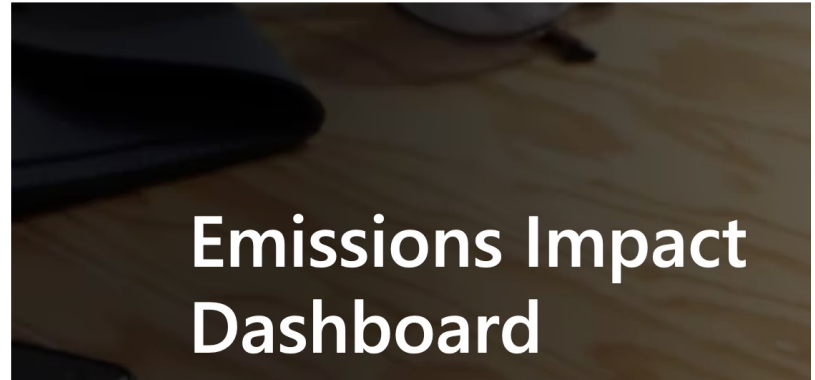


Cloud Jewels: Estimating kWh in the Cloud



By Emily Sommer, Mike Adler, John Perkins, Joshua Thiel, Hilary Young, Chelsea Mozen, Dany Daya, Katherine Sundstrom

Apr 23, 2020



Google Cloud

Overview Solutions **Products** Pricing Resources

Carbon Footprint

Catch up on the latest product launches, demos, and trainings from

Carbon accounting in the Cloud:
a methodology for allocating emissions across
data center users

Ian Schneider*, Taylor Mattia*†

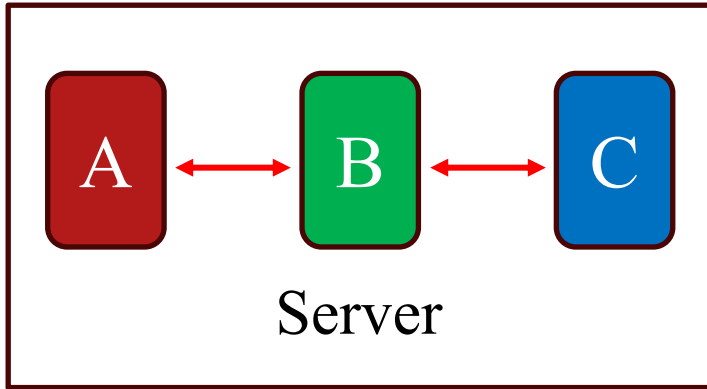
June 2024

Carbon Footprint

Measure, report, and reduce your cloud carbon emissions.

Existing attribution models may be unfair

Colocation effects



Poor proxies for embodied carbon

Google Cloud

Microsoft | Sustainability



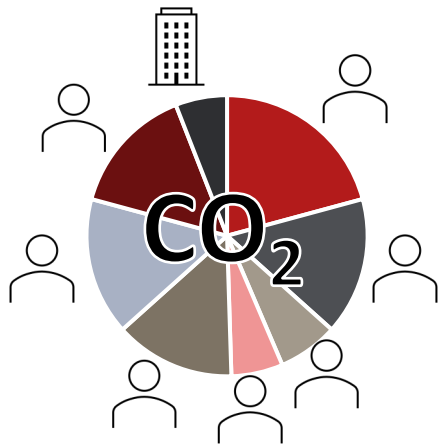
\neq embodied CO₂

Intel Xeon CPU: 792 USD/kgCO₂, 37 W/kgCO₂

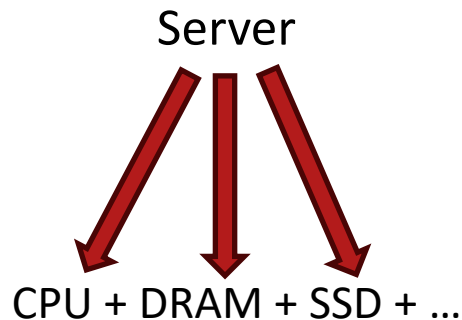
DDR4 DRAM: 4.29 USD/kgCO₂, 0.4 W/kgCO₂

Shapley value is a game theory solution for fair shared-cost attribution

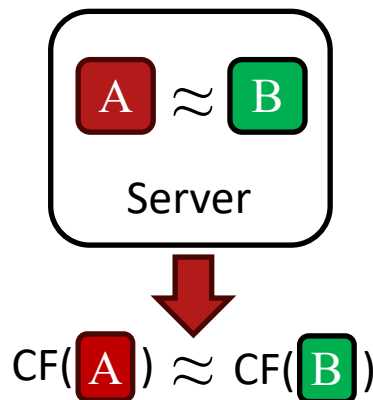
Efficiency



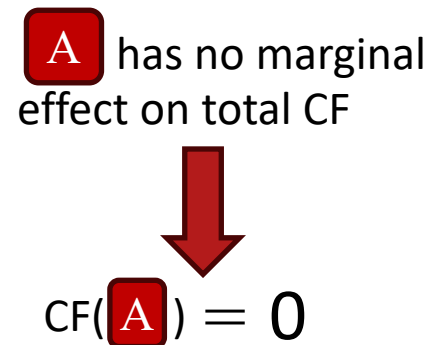
Linearity



Symmetry

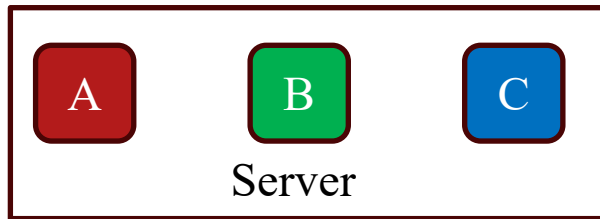


Null Player



Properties for Fair Attribution

Shapley value averages marginal contributions



What is A's share of the server carbon footprint (CF)?

$$CF(\{A\}) - CF(\{\})$$

$$CF(\{B, A\}) - CF(\{B\})$$

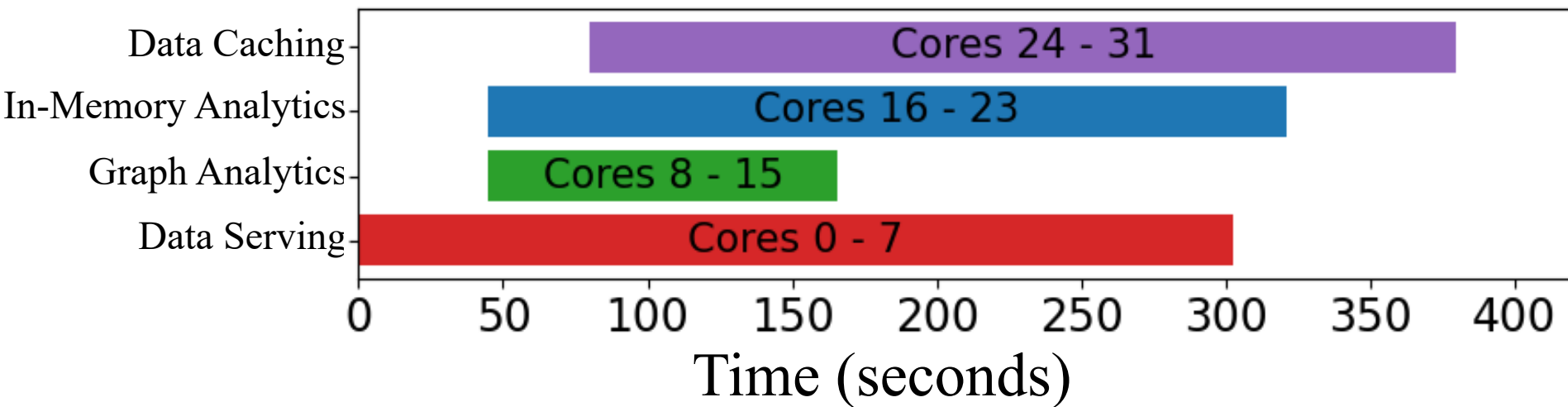
$$CF(\{C, A\}) - CF(\{C\})$$

$$CF(\{B, C, A\}) - CF(\{B, C\})$$

$$CF(\{C, B, A\}) - CF(\{C, B\})$$

Shapley value:
average of A's marginal
contribution across
all permutations

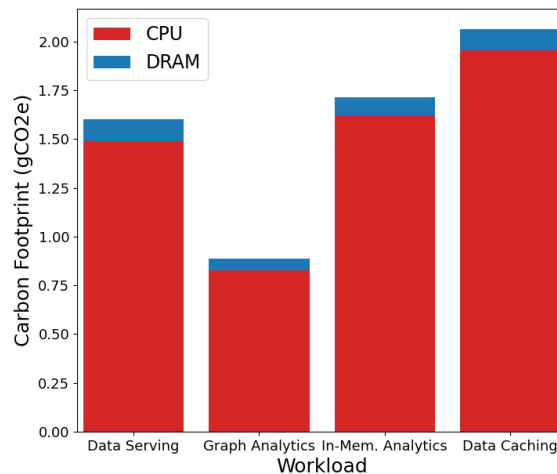
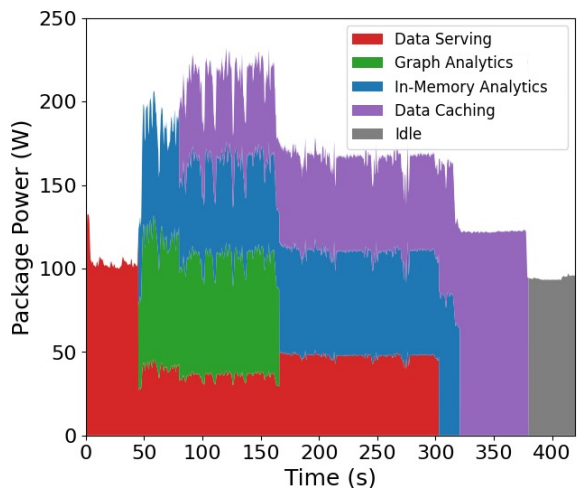
Case Study: Four CloudSuite 4.0 workloads on CloudLab Dell R650 Node



Shapley value power attribution accounts for colocation effects

Offline Power Profiles  Power Attribution  Operational Carbon Attribution

DS	GA	IA	DC	Power
				94.6 W
X				100.8 W
	X			137.0 W
...				
X	X	X		180.3 W
X	X	X	X	201.2 W

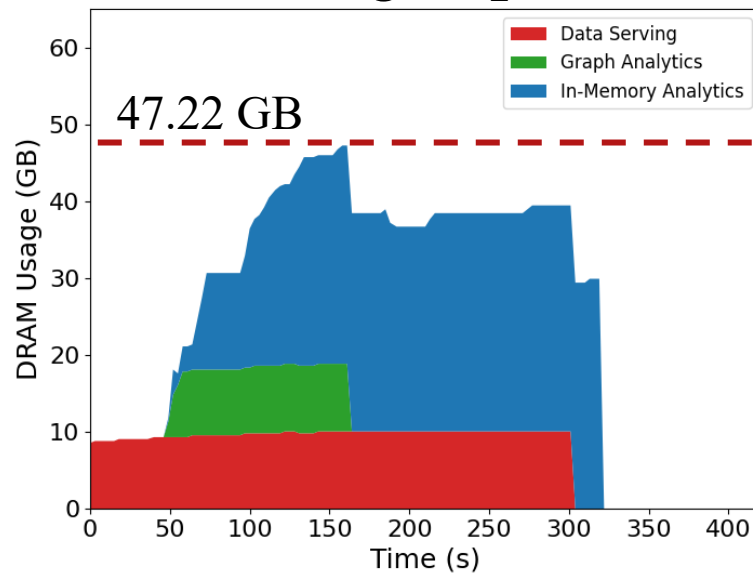
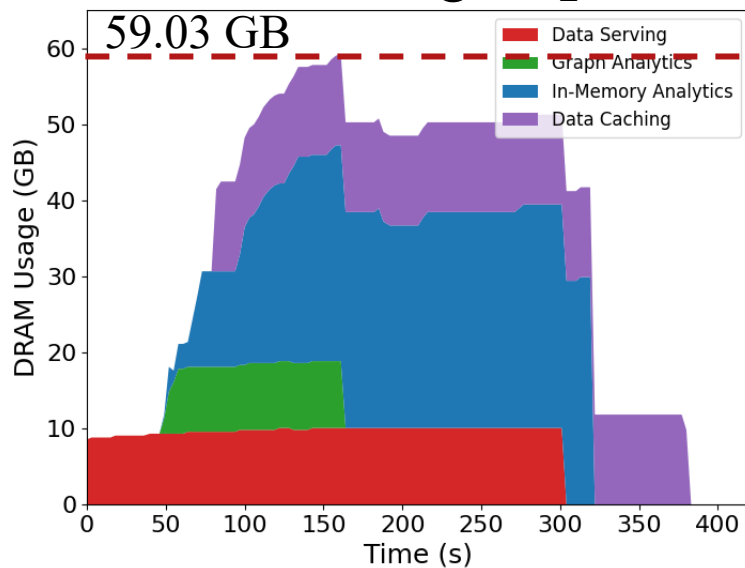


Shapley embodied carbon attribution based on resource utilization

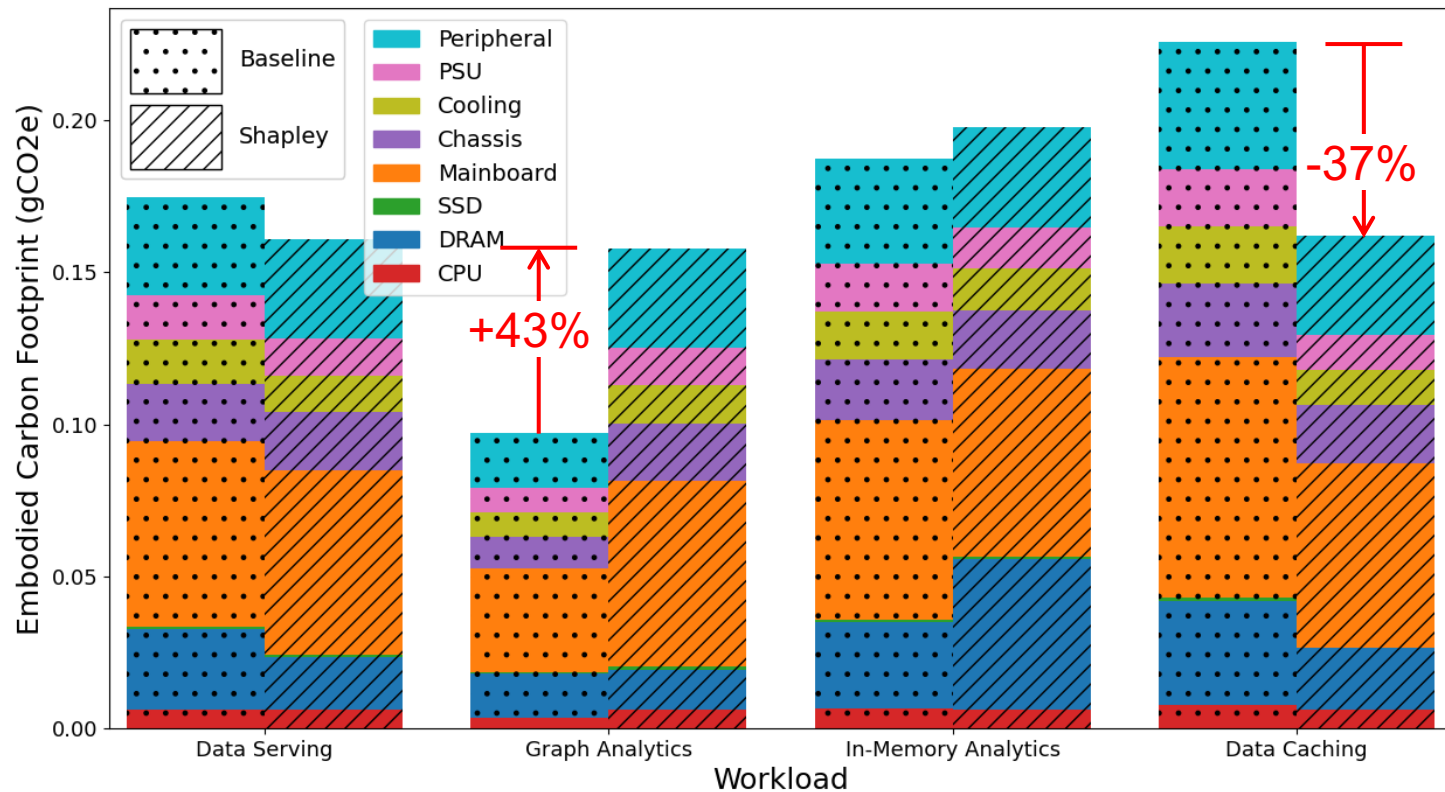
Example: DRAM @ 0.52 kgCO₂e/GB

$$CF_{\text{DRAM}}(\{\text{DS}, \text{GA}, \text{IA}, \text{DC}\}) - CF_{\text{DRAM}}(\{\text{DS}, \text{GA}, \text{IA}\})$$

30.70 kgCO₂e - 24.55 kgCO₂e = **6.15 kgCO₂e**



Per-resource Shapley attribution vs. baseline energy-proportional attribution



Limitations and Future Work

Limitation: Poor scalability

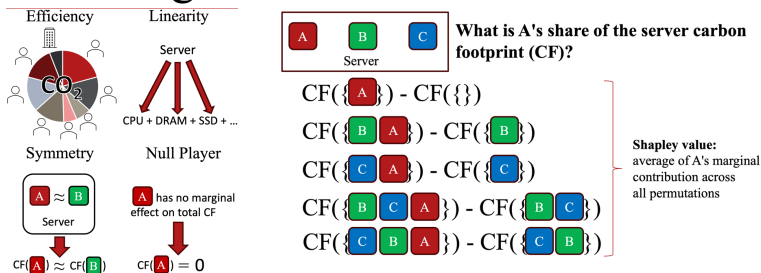
- Shapley methodology scales at $O(N^2)$ with number of workloads
- Offline profiling not scalable for larger number of workloads

Future work: Scalable Shapley carbon attribution

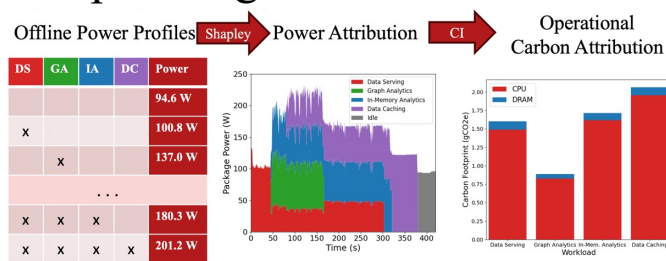
Future work: Workload optimizations with carbon attribution

Fair Carbon Attribution for Cloud Data Centers Using Shapley Values

Shapley values provide theoretical fairness guarantees for carbon attribution



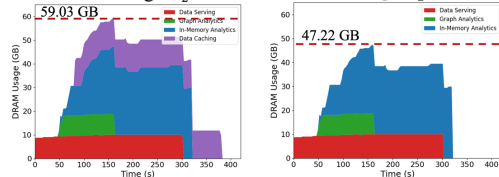
Operational carbon attribution using offline profiling



Embodied carbon attribution by tracking per-resource utilization

DRAM @ 0.52 kgCO₂e/GB

$$CF_{\text{DRAM}}(\{DS, GA, IA, DC\}) - CF_{\text{DRAM}}(\{DS, GA, IA\}) = 30.70 \text{ kgCO}_2\text{e} - 24.55 \text{ kgCO}_2\text{e} = 6.15 \text{ kgCO}_2\text{e}$$



Thank you!

Please connect with us via email at:

lxh4@cornell.edu (Leo)